

## Noam D. Elkies

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### BIOGRAPHICAL

Born Aug. 1966 in New York City  
Moved Dec. 1970 to Ramat Gan, Israel  
Returned Aug. 1978 to New York  
In Cambridge, Mass. since September 1985

### EDUCATION

Harvard University (GSAS), 9/1985–6/1987, M.A. in Mathematics 6/1986, Ph.D. in Mathematics 6/1987. Dissertation advised by Barry Mazur and Benedict Gross: *Supersingular primes of a given elliptic curve over a number field*.  
Columbia College, 9/1982–5/1985, B.A. *summa cum laude* in Mathematics and Music  
Stuyvesant High School, 9/1979–6/1982

### EMPLOYMENT

Harvard University, 7/1993–present, Professor (Mathematics)  
(Department head, 7/2012–6/2013)  
Harvard University, 7/1990–6/1993, Associate Professor (Mathematics), John L. Loeb Professor of the Natural Sciences  
Harvard University, 9/1987–6/1990, Junior Fellow (Mathematics)  
Institute for Defense Analyses, intermittently from 7/1986 to present, consultant  
Bell Laboratories, 7/1991, consultant

### DOCTORAL THESES ADVISED

Henry L. Cohn (2000): *New Bounds on Sphere Packing*  
David Y. Jao (2003): *Supersingular Primes for Rational Points on Modular Curves*  
Nicholas F. Rogers (2004): *Elliptic Curves  $x^3 + y^3 = k$  with High Rank*  
Abhinav Kumar (2006):  *$K3$  Surfaces of High Rank*  
Sonal Jain (2007): *Minimal Heights and Regulators On Elliptic Surfaces*  
Jeechul Woo (2011): *Arithmetic of Elliptic Curves and Surface: Descents and Quadratic Sections*  
Yevgeny Zaytman (2010):  *$K3$  surfaces of high Picard number and arithmetic applications*  
Nathan Kaplan (2012): *Rational Point Counts for del Pezzo Surfaces over Finite Fields and Coding Theory*

### SELECTED AWARDS AND HONORS

2011 - Louise and Richard Guy Lecture, University of Calgary  
2006 - K. Ireland Memorial Lecture, Univ. of New Brunswick  
2005 - Plenary address at British Mathematical Colloquium  
2005 - R.E. Phillips Lecture Series, Michigan State Univ.  
2004 - L.L. Conant Prize, American Mathematical Society  
2004 - L.R. Ford Award, Mathematical Association of America

2004 - Plenary address at annual meeting of the Israel Mathematical Union  
 2003 - Invited address at the 2003 AMS-MAA Joint Mathematics Meetings  
 1995 - Columbia University Medal of Excellence  
 1992 - Prix Peccot (Collège de France)  
 1991 - Packard Fellowship for Science and Engineering  
 1991 - Presidential Young Investigator  
 1991 - W.O. Baker Award for Initiatives in Research (National Academy of Sciences)  
 1990 - John L. Loeb Professor of the Natural Sciences (Harvard University)  
 1987 - Junior Fellow (Harvard University)  
 1985 - NSF Graduate Fellowship in Mathematics  
 1983–85 - Top 5 in 42nd, 43rd and 44th Putnam competitions; Putnam Fellowship for graduate study at Harvard  
 1985 - Valedictorian, Columbia College  
 1984 - Phi Beta Kappa (while in Junior year)  
 1982 - 1st in USA Math Olympiad; Gold Medal at International Math Olympiad  
 1982 - 8th in Westinghouse Science Talent Search  
 1981 - Tied for 1st in USA Math Olympiad; Gold Medal with perfect score at International Math Olympiad

## PUBLICATIONS

1. Integers expressible in the form  $a^4 + b^4$ , pages 22–28 in Vol. 3 of *Mathematical Buds* (H. Rudermand, ed.; Norman, Oklahoma: Mu Alpha Theta, 1984).
2. An improved lower bound on the greatest element of a sum-distinct set of fixed order, *J. Comb. Theory A* **41** (Jan. 1986), 89–94.
3. The existence of infinitely many supersingular primes for every elliptic curve over  $\mathbf{Q}$ , *Invent. Math.* **89** (1987), 561–568.
4. On  $A^4 + B^4 + C^4 = D^4$ , *Math. of Comp.* **51** (Oct. 88), 825–835.
5. Supersingular primes for elliptic curves over real number fields, *Compositio Math.* **72** (1989), 165–172.
6. The automorphism group of the modular curve  $X_0(63)$ , *Compositio Math.* **74** (1990), 203–208.
7. On the Hurwitz scheme and its monodromy (with D. Eisenbud, J. Harris, and R. Speiser), *Compositio Math.* **77** (1991), 95–117.
8. Distribution of supersingular primes, *Astérisque* **198-199-200** (1991; proceedings of Journées Arithmétiques 1989), 127–132.
9. On the packing densities of superballs and other bodies (with A.M. Odlyzko and J.A. Rush), *Invent. Math.* **105** (1991), 613–639.
10. ABC implies Mordell, *International Math. Research Notices* **7** (1991), 99–109.
11. Alternating sign matrices and domino tilings I, II (with G. Kuperberg, M. Larsen, and J. Propp), *J. Alg. Combinatorics* **1** (1992), 111–132 and 219–234.
12. Mordell–Weil lattices in characteristic 2: I. Construction and first properties, *International Math. Research Notices*, 1994 #8, 343–361; II. The Leech lattice as a Mordell–Weil lattice, *Inventiones Math.* **128** (1997), 1–8; III. A Mordell–Weil lattice of rank 128, *Experimental Math.* **10** (2001) #3, 467–473.

13. Wiles minus epsilon implies Fermat, pages 38–40 in *Elliptic Curves, Modular Forms, and Fermat's Last Theorem* (J. Coates and S.-T. Yau, eds.; Boston: International Press, 1995; proceedings of the 12/93 conference on elliptic curves and modular forms at the Chinese University of Hong Kong).
14. Heegner point computations, *Lecture Notes in Computer Science* **877** (proceedings of ANTS-1, 1994; L.M. Adleman, M.-D. Huang, eds.), 122–133.
15. On numbers and endgames, pages 135–150 in *Games of No Chance* (R.J. Nowakowski, ed.; MSRI Publ. #29, 1996 via Cambridge Univ. Press; proceedings of the 7/94 MSRI conference on combinatorial games). [math.CO/9905198](https://arxiv.org/abs/math.CO/9905198) on the arXiv.
16. A characterization of the  $\mathbf{Z}^n$  lattice, *Math. Research Letters* **2** (1995), 321–326.
17. Lattices and codes with long shadows, *Math. Research Letters* **2** (1995), 643–651.
18. Local statistics for random domino tilings of the Aztec diamond (with H. Cohn and J. Propp), *Duke Math. J.* **85** #1 (Oct. 1996), 117–166.
19. The exceptional cone and the Leech lattice (with B.H. Gross), *International Math. Research Notices* **1996** #14, 665–698.
20. Elliptic and modular curves over finite fields and related computational issues, pages 21–76 in *Computational Perspectives on Number Theory: Proceedings of a Conference in Honor of A.O.L. Atkin* (D.A. Buell and J.T. Teitelbaum, eds.; AMS/International Press, 1998).
21. Explicit modular towers, pages 23–32 in *Proceedings of the Thirty-Fifth Annual Allerton Conference on Communication, Control and Computing* (1997, T. Başar, A. Vardy, eds.), Univ. of Illinois at Urbana-Champaign 1998 ([math.NT/0103107](https://arxiv.org/abs/math.NT/0103107) on the arXiv).
22. Embeddings into the Integral Octonions (with B.H. Gross), *Pacific J. Math.*, Dec. 1997 (Olga Taussky-Todd Memorial Issue), 147–158.
23. Shimura curve computations, *Lecture Notes in Computer Science* **1423** (proceedings of ANTS-3, 1998; J.P. Buhler, ed.), 1–47 ([math.NT/0005160](https://arxiv.org/abs/math.NT/0005160) on the arXiv).
24. The still-Life density problem and its generalizations, pages 228–253 in *Voronoi's Impact on Modern Science, Book I* (P. Engel and H. Syta, eds.; Institute of Math., Kyiv 1998 = Vol.21 of *Proc. Inst. Math. Nat. Acad. Sci. Ukraine*). [math.CO/9905194](https://arxiv.org/abs/math.CO/9905194) on the arXiv.
25. Linearized algebra and finite groups of Lie type. I: Linear and symplectic groups, pages 77–107 in *Applications of curves over finite fields* (Seattle, 1997) = *Contemp. Math.* **245**, Providence: AMS, 1999.
26. The Klein quartic in number theory, pages 51–102 in *The Eightfold Way: The Beauty of Klein's Quartic Curve* (S. Levy, ed.; Cambridge Univ. Press, 1999; also online at the MSRI Publications site).
27. Rational points near curves and small nonzero  $|x^3 - y^2|$  via lattice reduction, *Lecture Notes in Computer Science* **1838** (proceedings of ANTS-4, 2000; W. Bosma, ed.), 33–63 (on the arXiv at [math.NT/0005139](https://arxiv.org/abs/math.NT/0005139)).
28. Explicit towers of Drinfeld modular curves, *Progress in Mathematics* **202** (2001), 189–198 (Proceedings of the 3rd European Congress of Mathematics, Barcelona, 7/2000: paper presented at the mini-symposium on “curves over finite fields and codes”; [math.NT/0005140](https://arxiv.org/abs/math.NT/0005140) on the arXiv).
29. Lattices, Linear Codes, and Invariants (2-part expository article), *Notices of the American Math. Society* **47** (2000), 1238–1245 and 1382–1391.

30. Cubic rings and the exceptional Jordan algebra (with B.H. Gross), *Duke Math. J.* **109** #2 (2001), 383–409.
31. Excellent nonlinear codes from modular curves, pages 200–208 in *STOC'01: Proceedings of the 33rd Annual ACM Symposium on Theory of Computing*, Hersonissos, Crete, Greece. Isomorphic with math.NT/0104115 on the arXiv.
32. On finite sequences satisfying linear recursions, *New York J. Math.* **8** (2002), 85–97 = <http://nyjm.albany.edu:8000/j/2002/8-5.html> (math.CO/0105007 on the arXiv).
33. Curves  $Dy^2 = x^3 - x$  of Odd Analytic Rank, *Lecture Notes in Computer Science* **2369** (proceedings of ANTS-5, 2002; C. Fieker and D.R. Kohel, eds.), 244–251. math.NT/0208056 on the arXiv.
34. Trinomials  $ax^7 + bx + c$  and  $ax^8 + bx + c$  with Galois Groups of Order 168 and  $8 \cdot 168$  (with N. Bruin), *Lecture Notes in Computer Science* **2369** (proceedings of ANTS-5, 2002; C. Fieker and D.R. Kohel, eds.), 172–188.
35. Appendix to “New Optimal Tame Towers of Function Fields over Small Finite Fields” by W.-C.W. Li, H. Maharaj, and H. Stichtenoth [identifying each of their four towers with a tower of classical modular curves], *Lecture Notes in Computer Science* **2369** (proceedings of ANTS-5, 2002; C. Fieker and D.R. Kohel, eds.), 384–389.
36. Higher Nimbers in pawn endgames on large chessboards, pages 61–78 in *More Games of No Chance* (R.J. Nowakowski, ed.; MSRI Publ. #42, 2002 via Cambridge Univ. Press; proceedings of the 7/00 MSRI workshop on combinatorial games). math.CO/0011253 on the arXiv.
37. The mathematical knight (with Richard Stanley), *Math. Intelligencer* **25** #1 (2003), 22–34.
38. New upper bounds on sphere packings I (with H. Cohn), *Annals of Math.* **157** (2003), 689–714 (math.MG/0110009 on the arXiv).
39. On the Sums  $\sum_{k=-\infty}^{\infty} (4k+1)^{-n}$ , *Amer. Math. Monthly* **110** #7 (Aug.-Sep. 2003), 561–573. Nearly isomorphic with math.CA/0101168 on the arXiv. Corrigenda: *Amer. Math. Monthly* **111** #5 (May 2004), 456.
40. On Elliptic  $K$ -curves, *Progress in Mathematics* **224** (2004), 81–91 (Proceedings of the 7/2002 Barcelona Euroconference on “Modular Curves and Abelian Varieties”, ed. J. Cremona, J.-C. Lario, J. Quer, and K. Ribet).
41. Curves of every genus with many points, II: Asymptotically good families (with E.W. Howe, A. Kresch, B. Poonen, J.L. Wetherell, and M.E. Zieve), *Duke Math. J.* **122** #2 (2004), 399–422 (math.NT/0208060 on the arXiv).
42. Elliptic Curves of Large Rank and Small Conductor (with M. Watkins), *Lecture Notes in Computer Science* **3076** (proceedings of ANTS-6, 2004; D. Buell, ed.), 42–56 (on the arXiv at math.NT/0403374).
43. Elliptic Curves  $x^3 + y^3 = k$  of High Rank (with N.F. Rogers), *Lecture Notes in Computer Science* **3076** (proceedings of ANTS-6, 2004; D. Buell, ed.), 184–193. math.NT/0403116 on the arXiv.
44. Gaps in  $\sqrt{n} \bmod 1$  and ergodic theory (with C.T. McMullen), *Duke Math. J.* **123** #1 (2004), 95–139.
45. The conjugate dimension of algebraic numbers (with N. Berry, A. Dubickas, B. Poonen, and C. Smyth), *Quart. J. Math.* **55** (2004), 237–252 (math.NT/0308069 on the arXiv).
46. New Directions in Enumerative Chess Problems, *Electronic J. of Combinatorics* **11(2)** (2004–2005) [Stanley-60 Festschrift], Article #4 (math.CO/0508645 on the arXiv).

47. Reduction of CM Elliptic Curves and Modular Function Congruences (with K. Ono and T. Yang), *International Math. Research Notices* **2005** #44, 2695–2707 (math.NT/0512350 on the arXiv).
48. Sylvester–Gallai Theorems for Complex Numbers and Quaternions (with L.M. Pretorius and K.J. Swanepoel), *Discrete and Computational Geometry* **35** #3 (3/2006), 361–373 (on the arXiv at math.MG/0403023).
49. The Mathieu group  $M_{12}$  and its pseudogroup extension  $M_{13}$  (with J.H. Conway and J.L. Martin), *Experimental Math.* **15** (2006) #2, 223–236 (math.GR/0508630 on the arXiv).
50. Points of Low Height on Elliptic Curves and Surfaces I: Elliptic surfaces over  $\mathbf{P}^1$  with small  $d$ , *Lecture Notes in Computer Science* **4076** (proceedings of ANTS-7, 2006; F. Hess, S. Pauli, and M. Pohst, eds.), 287–301. math.AG/0608593 on the arXiv.
51. Shimura Curves for Level-3 Subgroups of the (2,3,7) Triangle Group, and Some Other Examples, *Lecture Notes in Computer Science* **4076** (proceedings of ANTS-7, 2006; F. Hess, S. Pauli, and M. Pohst, eds.), 302–316. math.AG/0409020 on the arXiv.
52. On some points-and-lines problems and configurations, *Periodica Mathematica Hungarica* **53** #1–2 (2006), 133–148. math.MG/0612749 on the arXiv.
53. The  $D_4$  Root System Is Not Universally Optimal (with Henry Cohn, John H. Conway, and Abhinav Kumar), *Experimental Math.* **16** (2006) #3, 313–320. math.NT/0607447 on the arXiv.
54. Shimura Curve Computations Via K3 Surfaces of Néron-Severi Rank at Least 19, *Lecture Notes in Computer Science* **5011** (proceedings of ANTS-8, 2008; A.J. van der Poorten and A. Stein, eds.), 196–211. math.NT/0802.1301 on the arXiv.
55. About the cover: Rational curves on a K3 surface, pages 1–4 of Arithmetic Geometry: Proceedings of the Clay Mathematics Institute, Göttingen, 17 July – 11 August, 2006 (Henri Darmon, David Alexandre Ellwood, Brendan Hassett, and Yuri Tschinkel, eds.), *Clay Math. Proceedings* **8**, 2009. [www.math.rice.edu/~hassett/conferences/Clay2006/Elkies/CMIPelkies.pdf](http://www.math.rice.edu/~hassett/conferences/Clay2006/Elkies/CMIPelkies.pdf)
56. Refined Configuration Results for Extremal Type II Lattices of Ranks 40 and 80 (with Scott Duke Kominers), *Proceedings of the American Math. Society* **138** #1 (2010), 105–108. math.NT/0905.4306 on the arXiv.
57. On the Classification of Type II Codes of Length 24 (with Scott Duke Kominers), *SIAM J. Discrete Math.* **23** #4 (2010), 2173–2177. math.NT/0902.1942 on the arXiv.
58. Point configurations that are asymmetric yet balanced (with Henry Cohn, Abhinav Kumar, and Achill Schürmann), *Proceedings of the American Math. Society*, posted on March 23, 2010, PII S 0002-9939(10)10284-6; **138** #8 (August 2010), 2863–2872. math.MG/0812.2579 on the arXiv.
59. Weighted Generating Functions for Type II Lattices and Codes (with Scott Duke Kominers), pages 63–108 in *Quadratic and Higher Degree Forms* (Krishnaswami Alladi, Manjul Bhargava, David Savitt, and Pham Huu Tiep, eds.), *Developments in Mathematics* **31** 2013 (New York: Springer). math.NT/1111.2392 on the arXiv.

## OTHER

Extensive training as composer and pianist; some performances broadcast on television or radio in Israel and the United States; several commissions including *Shema* Op.34 for the Campaign for Choral Music at Harvard-Radcliffe and *Brandenburg Concerto #7* Op.49 for the Metamorphosen ensemble; Opera *Yossele Solovey* (libretto by J.Dauber after the novel by Sholem Aleichem) fully

staged at Harvard, 1999; *Four of my First* Op. 3 for piano, and *A Meditation on Mortality* Op. 31 #3 for mixed chorus, published respectively by Israeli Music Publications and Broude Brothers, Inc.

U.S. Chess master since 1986; Solving World Champion in 1996, and Solving Grandmaster since 2001. Chess publications include “Chess Art in the computer age” (*American Chess Journal* **2** (1995)), an endgame column in *Chess Horizons* running from 1988 to 1990, and numerous original endgame studies and chess problems. See also items 15, 36, 46 in the publication list above.

## REFERENCES

Prof. B. Mazur  
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Prof. B.H. Gross  
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